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Fig. 6. ORTEP plot (Johnson, 1967) of the crystal structure of BCT , showing some short intermolecular distances.

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# The Crystal Structure of Orthorhombic Antimony Trioxide, $\mathbf{S b}_{\mathbf{2}} \mathbf{O}_{\mathbf{3}}$ 

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The crystal structure of orthorhombic $\mathrm{Sb}_{2} \mathrm{O}_{3}$ has been reinvestigated with three-dimensional singlecrystal X-ray diffractometer data. The crystals are orthorhombic, space group Pccn, with $a=4.911$, $b=12.464$ and $c=5.412 \AA$. The structure was refined by full-matrix least-squares with 340 independent reflexions to $R=0.032$. The idealized geometry of the antimony coordination can be described as a tetrahedron with oxygens at three corners, at the approximately equal distances $1.98,2.02$ and $2.02 \AA$, and the lone pair of electrons of antimony at the fourth corner. The coordination polyhedra are joined by sharing corners to form double infinite chains with the lone pairs pointing out from the chains.

## Introduction

The structures of solid $\alpha$ - and $\beta$ - $-\mathrm{Bi}_{2} \mathrm{O}_{3}$ have recently been redetermined and refined (Malmros, 1970; Auri-
villius \& Malmros, 1972). Within this research programme, and also in order to obtain accurate antimony-(III)-oxygen distances, a refinement of orthorhombic $\mathrm{Sb}_{2} \mathrm{O}_{3}$ has been undertaken. The results of this in-
vestigation are in good agreement with the early structure determination reported by Buerger \& Hendricks (1938).

## Experimental

Orthorhombic $\mathrm{Sb}_{2} \mathrm{O}_{3}$ was prepared from a hydrochloric acid solution of $\mathrm{SbCl}_{3}$ and a boiling sodium carbonate solution as described by Debray (1866). Single crystals suitable for X-ray work were obtained by subliming the oxide at $600^{\circ} \mathrm{C}$ in nitı ogen (Bloom \& Buerger, 1937).

Weissenberg photographs taken with $\mathrm{Cu} K \alpha$ radiation indicated orthorhombic symmetry and showed systematic extinctions unique for space group Pcen (No. 56).

The unit-cell dimensions were determined by leastsquares refinement of 31 lines in the $\mathrm{CuK} \alpha_{1}(\lambda=$ $1 \cdot 54051 \AA$ ) powder pattern collected at room temperature in a Guinier-Hägg camera equipped with a quartz monochromator and with KCl as internal standard $(a=6.2929 \AA)$. The least-squares program PIRUM by Werner (1970) was used. The results were $a=4.911$ (1), $b=12.464$ (2), $c=5.412$ (1) $\AA$ and $V=$ $331 \cdot 3 \AA^{3}$. Standard deviations of the least significant digits are given in parentheses. With $Z=4$ the calculated density is $5.844 \mathrm{~g} \mathrm{~cm}^{-3}$, compared with 5.778 g $\mathrm{cm}^{-3}$ observed by Boullay (1830).

Intensities for a colourless, prismatic (110) crystal, elongated along $\mathbf{c}$, of approximate dimensions $0.02 \times$ $0.04 \times 0.12 \mathrm{~mm}$ were collected at room temperature, $22^{\circ} \mathrm{C}$, on an Enraf-Nonius computer-controlled fourcircle diffractometer, CAD4, with equatorial geometry. Graphite-monochromatized Mo $K \alpha$ radiation $(\lambda=$ $0.71069 \AA$ ) with a take-off angle of $5^{\circ}$ was used. The crystal was mounted with the $c$ axis tilted approximately $13^{\circ}$ from the $\varphi$ axis of the goniometer. The crystal orientation was determined, after centring 14 reflexions in the detector aperture, by least-squares determination of the matrix relating the indices of reflexion to the orthogonal goniometer-head coordinate system.

The $\omega-2 \theta$ scan technique was used with an $\omega$ range of $1.00^{\circ}$ and an aperture 4.5 mm wide and 6.0 mm high, corresponding to an angle in the equatorial plane as seen from the crystal of $1.5^{\circ}$. The distance X-ray source to crystal was 216 mm . A minimum net count of 3000 was attained within a maximum measuring time of 5 min . The scan speed was calculated from the net intensity in a fast prescan. The scan was continuous and the background counts were taken at each end of the scan interval with stationary crystal-stationary counter for $\frac{1}{4}$ of the time spent on the scan. The measurements were repeated and the corresponding counts were added in the output from the diffractometer.

Two octants of reciprocal space out to $(\sin \theta) / \lambda=$ 0.70 were examined, part of one octant being measured twice. The total number of reflexions was 1195 of which 403 were considered not above background by giving net counts less than 10 in the fast prescan of 9 s . Another 59 intensities were considered unobserved,
being weaker than $3 \sigma(I)$, where $I$ is the intensity and $\sigma(I)$ its standard deviation. $I$ was calculated from $I=$ $\left[T-k\left(B_{1}+B_{2}\right)\right] / t$ and $\sigma(I)$ from $\sigma^{2}(I)=\left[T+k^{2}\left(B_{1}+\right.\right.$ $\left.\left.B_{2}\right)\right] / t^{2}$, where $T, B_{1}$ and $B_{2}$ are the peak counts and the two background counts respectively. The factor $k$ is the ratio of scan time to total background measuring time, i.e. in this experiment $k=2$, and $t$ is a factor proportional to the measuring time. The remaining 733 intensities were corrected for Lorentz, polarization and absorption effects with the program $D A T A P C$ which is a modification by the author of a program originally written by Coppens, Leiserowitz \& Rabinovich (1965). The polarization factor used was the one for ideally mosaic crystals, $p=\left(1+\cos ^{2} 2 \theta_{M} \cos ^{2} 2 \theta\right) /\left(1+\cos ^{2} 2 \theta_{M}\right)$. The linear absorption coefficient for Mo $K \alpha$ radiation is $150 \mathrm{~cm}^{-1}$. The transmission factors were in the range 0.53-0.73.

Two control reflexions, 240 and 080, were measured at 30 min intervals to check for crystal decomposition and radiation stability. The mean decrease in intensity over the whole exposure time, 54 h , was $4 \%$ for both control reflexions. Maximum intensity variations over the data collection period, 90 h , were 7 and $8 \%$ respectively corresponding to approximately 7 and $8 \sigma(I)$. All intensities and their variances were scaled according to these control reflexions.

The structure refinement was started with the atomic coordinates given by Buerger \& Hendricks (1938) (cf. Table 1) and isotropic temperature factors. Antimony and one of the oxygen atoms occupy the general eightfold point position, whereas the other oxygen atom is located on a twofold axis in a fourfold point position. The least-squares program used was LINUS by Coppens \& Hamilton (1970). The function minimized was $\sum w_{i}\left(\left|F_{o}\right|-\left|F_{c}\right|\right)^{2}$ where the weights, $w_{i}$, were calculated from $w_{i}^{-1}=\sigma^{2}\left(F_{o}^{2}\right) / 4 F_{o}^{2}+c F_{o}^{2}$. The constant $c$ was chosen so as to given the most constant averages of $w_{i}\left(\left|F_{o}\right|-\left|F_{c}\right|\right)^{2}$ over ranges of $F$ and $\sin 0$. A value of $c=0.00025$ was used. The scattering factors were those of Doyle \& Turner (1968) for neutral atoms antimony and oxygen. An anomalous dispersion correction for antimony (Cromer \& Liberman, 1970) was included. The process of refinement can be followed in Table 2. The 733 observed reflexions refined to $R=$ $\sum\left|\left|F_{o}\right|-\left|F_{c}\right|\right| / \sum\left|F_{o}\right|=0.039$ with all atoms anisotropic and an isotropic correction for secondary extinction. The extinction parameter was $g=3 \cdot 2$ (3). $10^{3}$. The structure factor of the reflexion suffering most from extinction was corrected by $29 \%$. After averaging of all equivalent reflexions the final $R$ was 0.032 for 340 reflexions. The shifts in the last cycle of refinement

Table 1. Fractional coordinates of orthorhombic $\mathrm{Sb}_{2} \mathrm{O}_{3}$ according to Buerger \& Hendricks (1938)

|  | $x$ | $y$ | $z$ |
| :--- | :--- | :--- | ---: |
| Sb | 0.044 | 0.128 | 0.179 |
| $\mathrm{O}(1)$ | 0.25 | 0.25 | 0.029 |
| $\mathrm{O}(2)$ | 0.147 | 0.058 | -0.139 |

Table 2. Summary of the refinement

| Parameters refined | Number of observations ( $m$ ) | Number of parameters refined ( $n$ ) | $S$ | $R_{\text {w }}$ | $R$ | $\begin{aligned} & \sigma(z) \text { for } \\ & \mathrm{O}(1) \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (a) overall scale factor, atomic coordinates, isotropic temperature factors | 733 | 11 | $3 \cdot 13$ | 0.071 | 0.060 | $0 \cdot 0024$ |
| (b) same as (a) but anisotropic temperature factor for Sb . | 733 | 16 | $2 \cdot 51$ | 0.057 | 0.048 | 0.0019 |
| (c) same as (b) but also isotropic extinction correction | 733 | 17 | 2.05 | 0.046 | 0.040 | 0.0016 |
| (d) same as (c) but anisotropic temperature factors for $\mathrm{O}(1)$ and $\mathrm{O}(2)$ | 733 | 25 | 2.00 | 0.045 | 0.039 | 0.0014 |
| (e) all equivalent reflexions averaged. | 340 | 24 | 1.59 | 0.037 | 0.032 | 0.0015 |

$S=\left[\sum w\left(\left|F_{o}\right|-\left|F_{c}\right|\right)^{2} /(m-n)\right]^{1 / 2}, R_{w}=\left(\sum w\left(\left|F_{o}\right|-\left|F_{c}\right|\right)^{2} / \sum w\left|F_{o}\right|^{2}\right)^{1 / 2}, R=\Sigma| | F_{o}\left|-\left|F_{c}\right| / \Sigma\right| F_{o} \mid, \sigma(z)$ for $\mathrm{O}(1)$ is the standard deviation of fractional coordinate $z$ for atom $\mathrm{O}(1)$.

Table 3. Final positional and thermal parameters
The form of the temperature factor is $\exp \left[-\left(h^{2} \beta_{11}+k^{2} \beta_{22}+l^{2} \beta_{33}+2 h k \beta_{12}+2 k l \beta_{23}+2 h l \beta_{13}\right)\right]$. The $\beta_{i j}$ 's have been multiplied by $10^{4}$.
Least-squares standard deviations are given in parentheses.

|  | $x$ | y | $z$ | $\beta_{11}$ | $\beta_{22}$ | $\beta_{33}$ | $\beta_{12}$ | $\beta_{13}$ | $\beta_{23}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Sb | 0.04149 (11) | $0 \cdot 12745$ (4) | $0 \cdot 17845$ (9) | $122 \cdot 1$ (2.5) | $17 \cdot 4$ (0.4) | $62 \cdot 0(1 \cdot 9)$ | $9 \cdot 7(0 \cdot 8)$ | 7.4 (1.6) | $5 \cdot 1(0 \cdot 7)$ |
| $\mathrm{O}(1)$ | 0.25 | 0.25 | 0.0229 (15) | 250 (43) | 15 (4) | 40 (24) | -5 (12) | 0 | 0 |
| $\mathrm{O}(2)$ | $0 \cdot 1520$ (15) | 0.0591 (4) | -0.1446 (10) | 121 (26) | 17 (3) | 73 (19) | -17(8) | -42 (19) | 10 (7) |

were for all parameters less than 0.01 times their standard deviations. At this stage a difference synthesis showed residuals near the antimony position ranging from -1.9 to 1.7 e $\AA^{-3}$. The largest residuals elsewhere were $1 \cdot 1 \mathrm{e} \AA^{-3}$. The final positional and thermal parameters and their estimated standard deviations are given in Tables 3 and 4. Observed and calculated structure factors are listed in Table 5. Some selceted distances and angles are given in Table 6. These were calculated by program ORFFE (Busing \& Levy, 1964), using the complete variance-covariance matrix to determine standard deviations.

Table 4. Root-mean-square amplitudes along the principal axes of the thermal vibration ellipsoids

|  | $R_{1}(\AA)$ | $R_{2}(\AA)$ | $R_{3}(\AA)$ |
| :--- | :--- | :--- | :--- |
| Sb | $0.0928(17)$ | $0.1070(16)$ | $0.1334(13)$ |
| $\mathrm{O}(1)$ | $0.077(24)$ | $0.108(17)$ | $0.175(16)$ |
| $\mathrm{O}(2)$ | $0.082(17)$ | $0.095(14)$ | $0.152(12)$ |

## Discussion

The structure consists of infinite chains of composition $\mathrm{Sb}_{2} \mathrm{O}_{3}$ running parallel to $\mathbf{c}$. Part of such a chain is shown in Fig. 1. Three oxygen atoms are coordinated all to one side of antimony, with a stereochemically active lone pair of electrons completing a somewhat distorted tetrahedron. Three-valent antimony with this one-sided coordination also occurs in compounds such as cubic $\mathrm{Sb}_{2} \mathrm{O}_{3}$ (Bozorth, 1923) and $\mathrm{SbF}_{3}$ (Edwards, 1970). Every oxygen is shared between two antimony atoms and the three antimony-oxygen distances, 2.023 (4), 2.019 (6) and 1.977 (7) $\AA$, are very similar. In fact, assuming an underestimation of the standard

Table 5. Observed and calculated structure factors
The columns list $h, F_{o}$ and $F_{c}$.



Fig. 1. A stereoscopic view down [100] of part of an infinite chain in orthorhombic $\mathrm{Sb}_{2} \mathrm{O}_{3}$, drawn by program ORTEP (Johnson, 1965). The thermal vibration ellipsoids have been scaled to include $95 \%$ probability.

Table 6. Interatomic distances and bond angles
All distances shorter than $3.0 \AA$ are included. The superscripts refer to atoms at the following equivalent positions: $x, y, z$; (i) $\frac{1}{2}-x, \frac{1}{2}-y, z$; (ii) $-x,-y,-z$; (iii) $\frac{1}{2}-x, y, \frac{1}{2}+z$ and (iv) $\frac{1}{2}-x, y, z-\frac{1}{2}$, where $x, y, z$ refer to the coordinates listed in Table 4. Standard deviations are given in parentheses.

| (a) Distances |  |
| :---: | :---: |
| $\mathrm{Sb}-\mathrm{O}(1)$ | 2.023 (4) $\AA$ |
| $\mathrm{Sb}-\mathrm{O}\left(1^{\text {iii }}\right)$ | $2 \cdot 619$ (6) |
| $\mathrm{Sb}-\mathrm{O}(2)$ | 2.019 (6) |
| $\mathrm{Sb}-\mathrm{O}\left(2^{11}\right)$ | 2.518 (6) |
| $\mathrm{Sb}-\mathrm{O}\left(2^{\text {iiI }}\right.$ ) | 1.977 (7) |
| $\mathrm{O}(1)-\mathrm{O}\left(1^{\text {iif }}\right), \mathrm{O}\left(1^{\text {iv }}\right)$ | $2 \cdot 706$ (1) |
| $\mathrm{O}(1)-\mathrm{O}(2)$ | 2.592 (6) |
| $\mathrm{O}(2)-\mathrm{O}\left(2^{\text {i }}\right.$ ) | $2 \cdot 617$ (12) |
| $\mathrm{O}(2)-\mathrm{O}\left(2^{\text {iii }}\right), \mathrm{O}\left(2^{\text {iv }}\right)$ | $2 \cdot 872$ (5) |

The shortest antimony-antimony distance is $\mathrm{Sb}^{-\mathrm{Sb}^{\mathrm{iii}} \text { of }}$ $3 \cdot 394$ (1) $\AA$.
(b) Angles

| $\mathrm{O}(1)-\mathrm{Sb}-\mathrm{O}(2)$ | $79.8(3)^{\circ}$ |
| :---: | :---: |
| $\mathrm{O}(1)-\mathrm{Sb}-\mathrm{O}\left(2^{\text {ii }}\right.$ ) | 98.1 (2) |
| $\mathrm{O}(2)-\mathrm{Sb}-\mathrm{O}\left(2^{\text {li }}\right.$ ) | 91.9 (2) |
| $\mathrm{Sb}--\mathrm{O}(1)-\mathrm{Sb}^{\text {i }}$ | $130 \cdot 8$ (4) |
| $\mathrm{Sb}-\mathrm{O}(2)-\mathrm{Sb}^{\text {iii }}$ | $116 \cdot 2$ (3) |

deviations by a factor of two the differences are not significant at the $5 \%$ level. The weighted mean $\mathrm{Sb}-\mathrm{O}$ bond distance is $2 \cdot 013$ (6) $\AA$.

The antimony atom has two next-nearest oxygen neighbours at distances $2 \cdot 619$ (6) and 2.518 (6) $\AA$ in the same chain and in a neighbouring chain, respectively. The latter distance probably results from an antimony-oxygen interaction and this would thus contribute to the van der Waals forces to hold the structure together. The interlayer bonding is however weak and accounts well, as pointed out by Buerger \& Hen-
dricks, for the perfect prismatic cleavage of the crystals.
The structure can also be discussed with respect to the volume per anion. It has recently been shown by Andersson, Åström, Galy \& Meunier (1973) that for many solid oxides, or oxide fluorides of $\mathrm{Sb}^{3+}, \mathrm{Pb}^{2+}$, $\mathrm{Bi}^{3+}$ and $\mathrm{Te}^{4+}$ the volume of the lone pair and its cation is of the size of that of an anion. If simply the unit-cell volume of orthorhombic $\mathrm{Sb}_{2} \mathrm{O}_{3}$ is divided by its contents of antimony lone pairs and oxygens the resulting volume per anion is $16 \cdot 6 \AA^{3}$. When comparing with the corresponding figure $17 \cdot 3 \AA^{3}$ for cubic $\mathrm{Sb}_{2} \mathrm{O}_{3}$ one can conclude that the orthorhombic polymorph should be the high-pressure form. The magnitude of these figures also compares well with the corresponding figures $16 \cdot 6,16 \cdot 6$ and $16 \cdot 7 \AA^{3}$ for $\mathrm{SbF}_{3}$ (Edwards, 1970) and $L$ - and $M$-SbOF (Åström, 1972; Åström \& Andersson, 1973), respectively.

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